

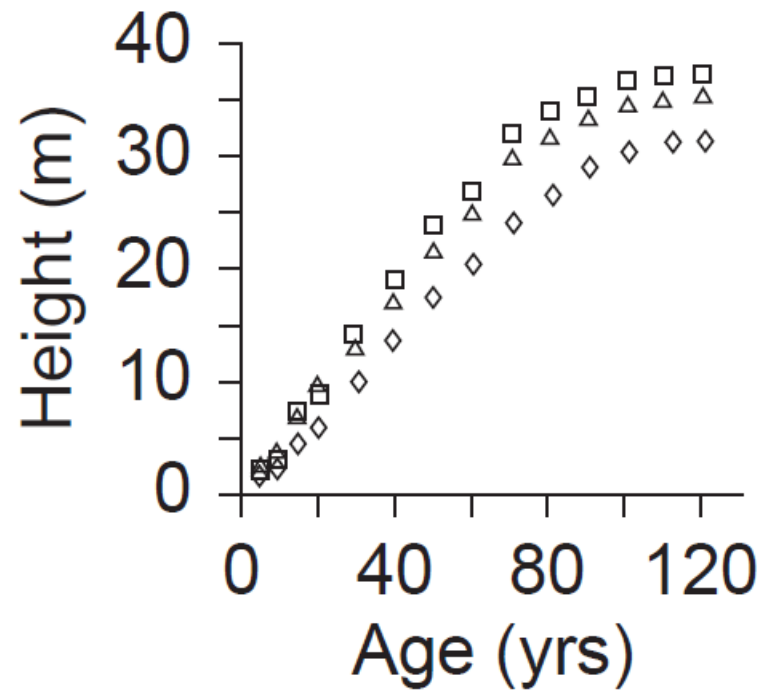
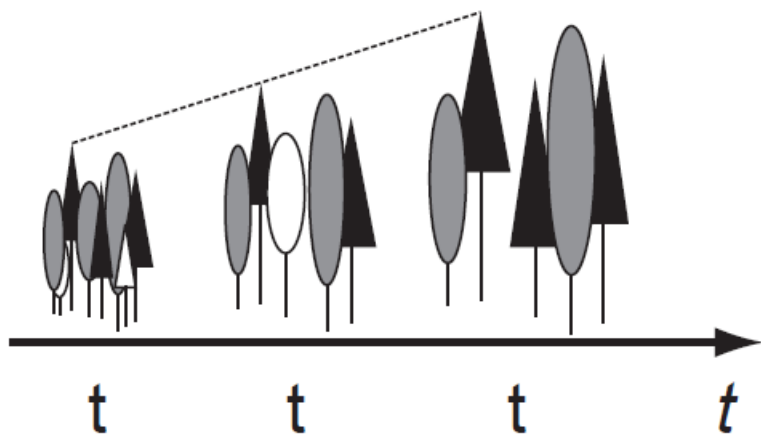
**Methods to study the evolution of
tree and stand variables over time**

Where do we get the data for growth studies?

✗ In permanent and interval plots

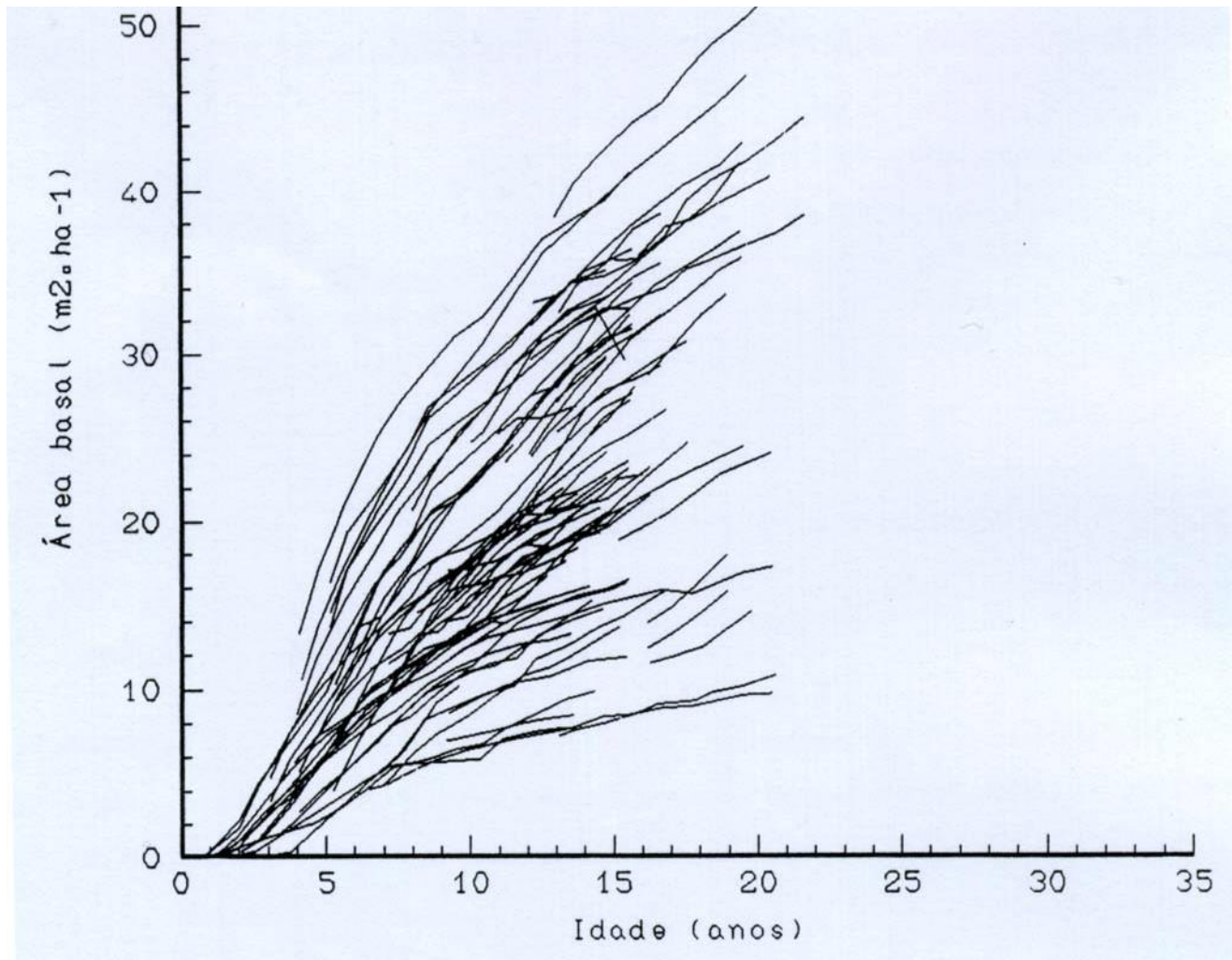
- ✓ Plots established with the objective of measuring growth in stands managed according to “current” practices
 - Permanent plots follow the stand during a long period, eventually the whole life of the stand

Permanent plots



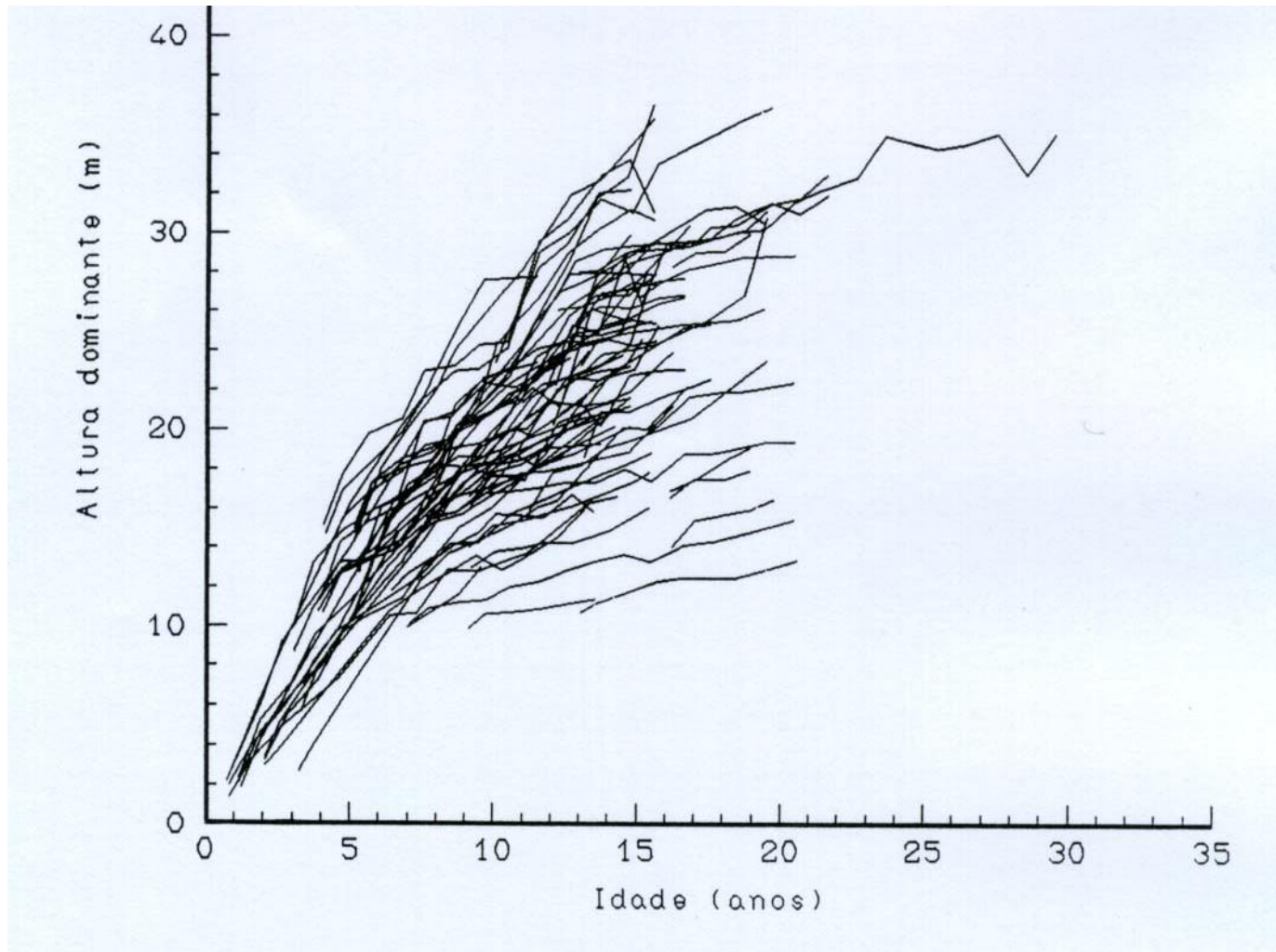
Examples of permanent plot data

G - eucalyptus



Examples of permanent plot data

h_{dom} - eucalyptus

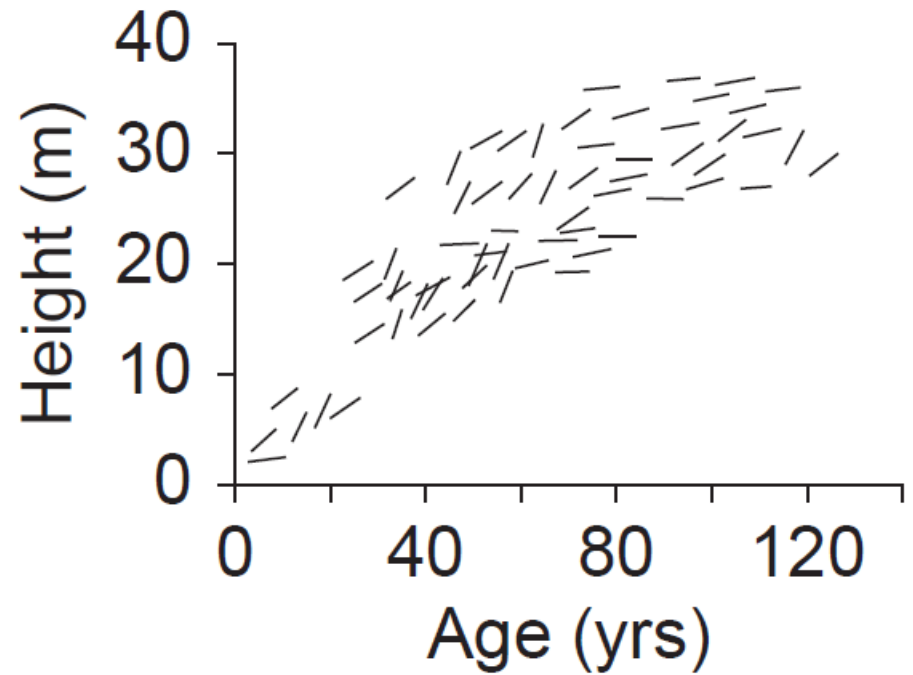
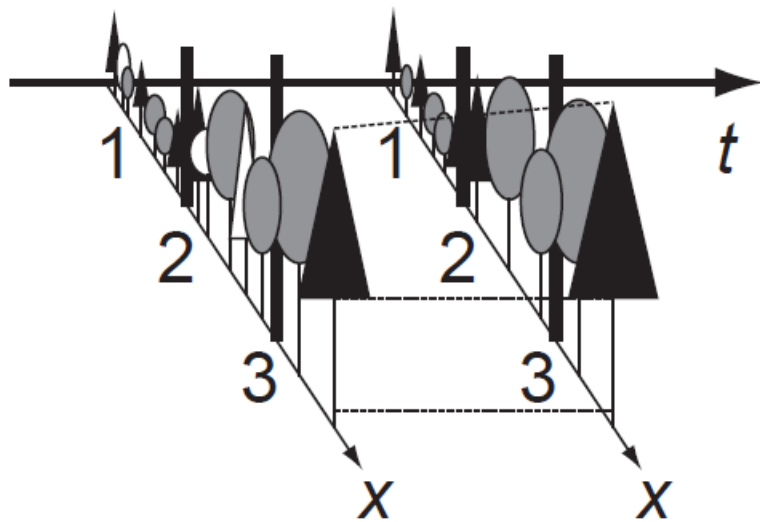


Where do we get the data for growth studies?

✗ In permanent and interval plots

- ✓ Plots established with the objective of measuring growth in stands managed according to “current” practices
 - Permanent plots follow the stand during a long period, eventually the whole life of the stand
 - Interval plots follow the stand during a limited interval, but they are remeasured at least once

Interval plots



Where do we get the data for growth studies?

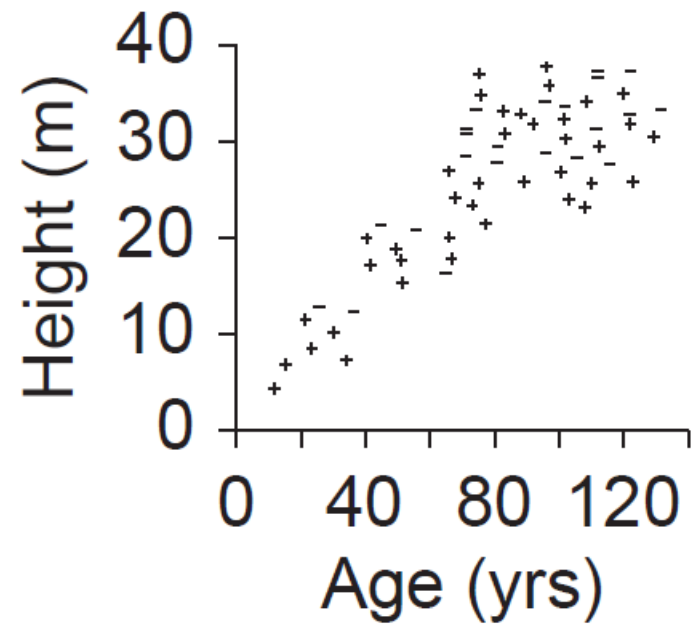
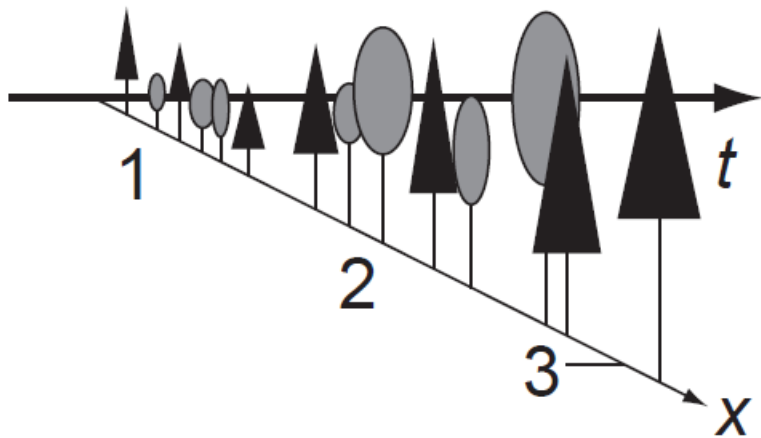
✗ In permanent and interval plots

- ✓ Plots established with the objective of measuring growth in stands managed according to “current” practices
 - Permanent plots follow the stand during a long period, eventually the whole life of the stand
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✗ In temporary plots

- ✓ Plots that are measured just at one point in time

Temporary plots



Where do we get the data for growth studies?

- ✗ In designed silviculture and genetic trials
 - ✓ Trials purposively established to study the impact of silvicultural treatments and/or genetic material on tree and stand growth
- ✗ From continuous forest inventory data
- ✗ From stem analysis

ANALYSIS OF MEASURED RESULTS

**PERMANENT
PLOTS**

FIELD TRIALS

Data for
construction and
validation

Indication for the
need to obtain new
data

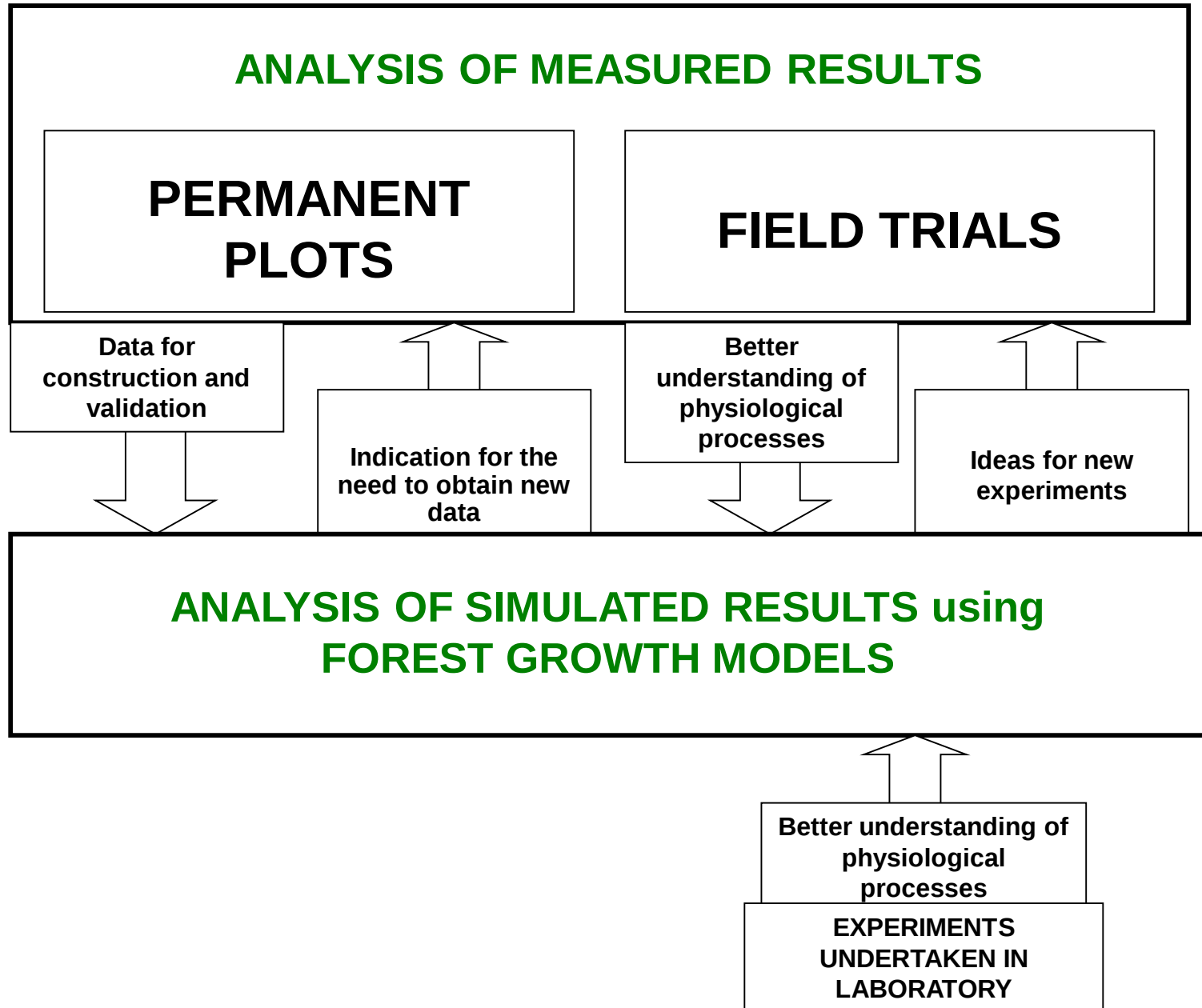
Better
understanding of
physiological
processes

Ideas for new
experiments

ANALYSIS OF SIMULATED RESULTS using FOREST GROWTH MODELS

Better understanding of
physiological
processes

**EXPERIMENTS
UNDERTAKEN IN
LABORATORY**



Stem analysis

- ✗ Stem analysis is the study of tree growth from the analysis and measurement of the growth rings
- ✗ It is restricted to the species whose wood exhibits clear growth rings and to the regions with a climate that implies a clear stop on growth
- ✗ Two types of stem analysis:
 - ✓ Partial - analysis of increment cores at dbh level
 - ✓ Total - analysis of several tree discs along the stem

Partial stem analysis

Stand table projection

- ✗ It is usually used for short term projections of forest inventory data:
 1. During the forest inventory an increment bore is taken in some “sample” trees
 2. Diameter growth of wood in the last k years (usually 5 years) is measured in the increment bore from each tree and converted to diameter growth
 3. Estimate the diameter growth (id_j) of the average tree of each diameter class (j)

Increment borer



Partial stem analysis

Stand table projection

✗ It includes several steps:

1. Start by computing the stand table (number of trees per diameter class) from forest inventory data
2. Estimate mortality in each diameter class and compute the future number of trees
3. Compute the growth index or ratio between id_j and the width of the class - this index allows the computation of the number of trees that stay in the class and the ones that move 1 or 2 classes

Partial stem analysis

Stand table projection

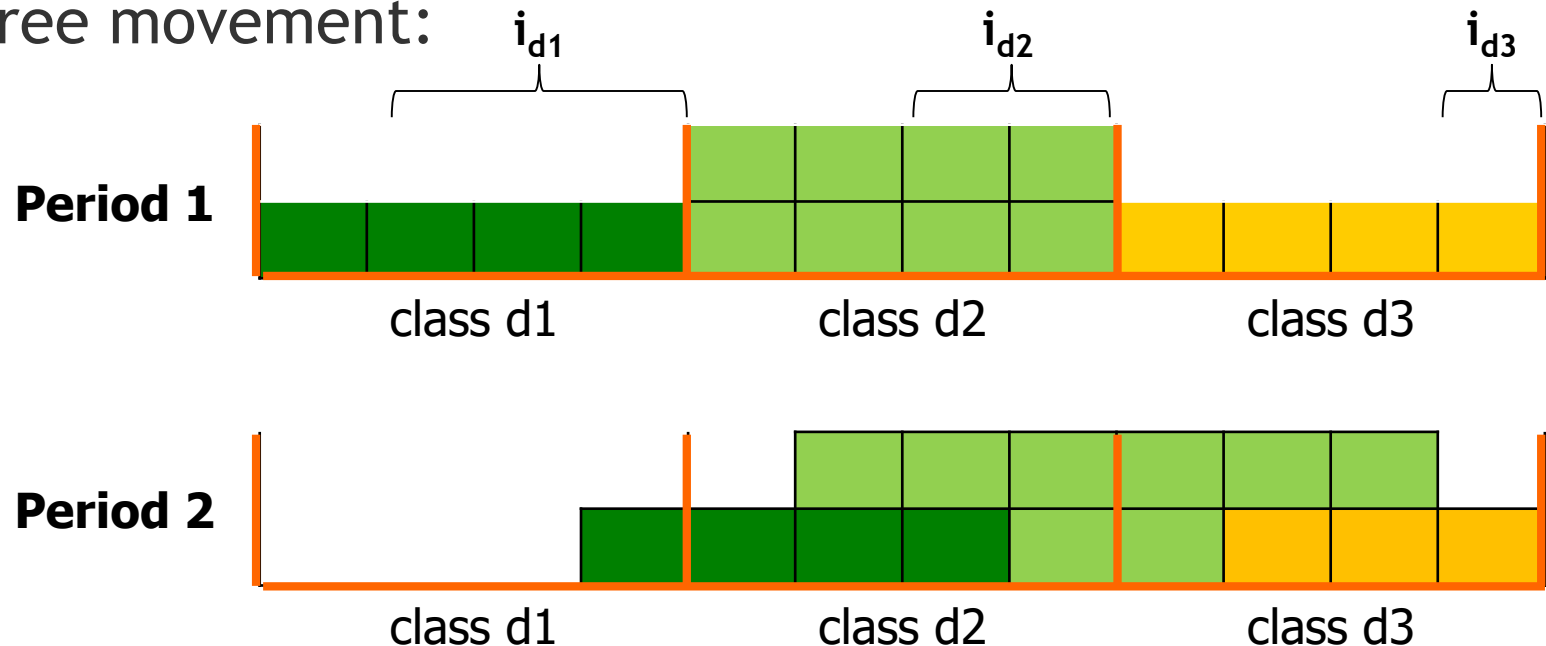
✕ Computation of growth index:

- ✓ Assumes that trees inside a dbh class have an uniform distribution
- ✓ Estimate the diameter increment in k years of each dbh class (i_d)
- ✓ All trees inside a dbh class $[d_1; d_2[$ with $d > d_2 - i_d$, after k years will be in the next class

Partial stem analysis

Stand table projection

✗ Tree movement:



✓ Note that now the trees are not equally distributed but this assumption will hold for the next period projection

Partial stem analysis

Stand table projection

class j (5 cm)	N _{j1996} after mortality	d increment id ₅ (cm)	Growth index		Movements			N _{j2001}
			P ₁	P ₂	stay	1 class	2 classes	
ingrowth						100		
5	102	3.80	0.76	0	24.48	77.52	0	
10	59	3.80	0.76		14.10	44.84		
15	53	3.85	0.77		12.10	40.81		
20	59	3.85	0.77	0	12.10	45.42	0	
25	58	3.85	0.77	0			0	
30	22	3.90	0.78	0	4.84	17.16	0	
35	1	3.90	0.78	0	0.22	0.78	0	
40	0							
45								
Total								

$$=3.80/5\text{cm}$$

$$=102-24.48$$

$$=102*(1-0.76)$$

Future
number of
trees alive
in each
class

Increment
in
diameter
for the
period

Partial stem analysis

Stand table projection

- ✗ We should also take into account the ingrowth
 - ✓ trees that achieve the lower limit of the first diameter class and must be added to the stand

Partial stem analysis

Stand table projection

class j (5 cm)	N _{j1996} after mortality	d increment id ₅ (cm)	Growth index		Movements			N _{j2001}
			P ₁	P ₂	stay	1 class	2 classes	
ingrowth						100		
5	102	3.80	0.76	0	24.48	77.52	0	124
10	59	3.80	0.76	0	14.16	44.84	0	92
15	53	3.85	0.77	0	12.19	40.81	0	57
20	59	3.85	0.77	0	13.57	45.43	0	54
25	58	3.85	0.77	0	13.34	44.66		59
30	22	3.90	0.78	0	4.84	17.16		50
35	1	3.90	0.78	0	0.22	0.78	0	17
40	0							1
45								
Total	354							454

=24+100

Partial stem analysis

Stand table project

- ✗ To estimate volume (or biomass) increment:
 - ✓ Estimate the height of the average tree in each diameter class using a height-diameter curve
 - ✓ Estimate the respective volume with a volume equation
 - ✓ Estimate the volume in each point in time using the stand tables
 - ✓ Obtain the volume (biomass) growth by difference

Partial stem analysis

Stand table projection

class j (5 cm)	N _{j1996} after mortality	N _{j2001}	h _j m	v _j m ³ /tree	V _{j1996} m3/ha	V _{j2001} m3/ha	
ingrowth							
5	102	124	6.8	0.0070	0.71	0.87	
10	59	92	12.1	0.0470	2.77	4.30	=0.0070*124
15	53	57	16.2	0.1387	7.35	7.91	
20	59	54	19.7	0.2939	17.34	15.98	
25	58	59	22.5	0.5204	30.18	30.58	
30	22	50	24.9	0.8237	18.12	40.77	
35	1	17	27.0	1.2080	1.21	20.99	
40	0	1	28.7	1.6763	0.00	1.31	V growth
45						0	m ³ /ha
Total	354	454			78	123	45

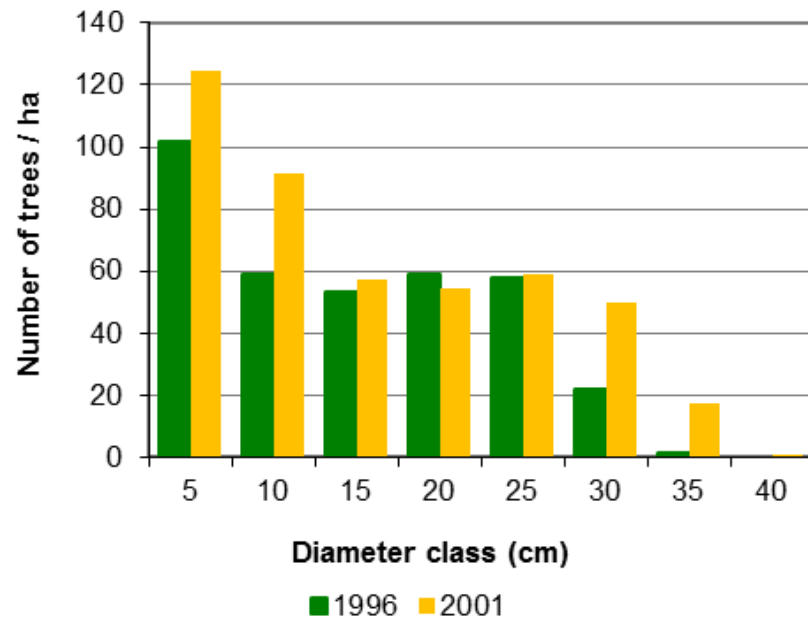
Tree height with a height-diameter curve: $h = d / (0.64212 + 0.01874 * d)$

Total volume with a volume equation: $v = 0.00005126 d^{2.0507} h^{0.8428}$

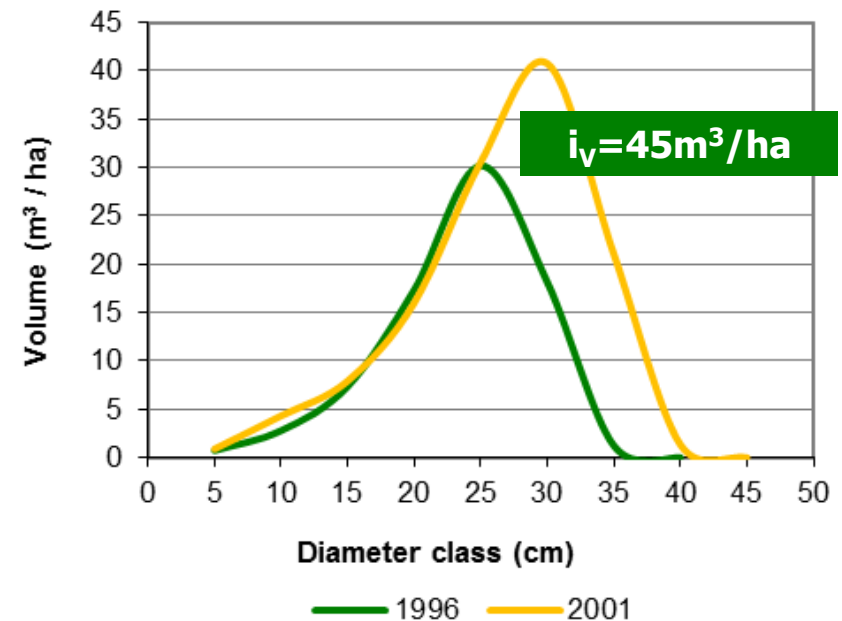
Partial stem analysis

Stand table projection

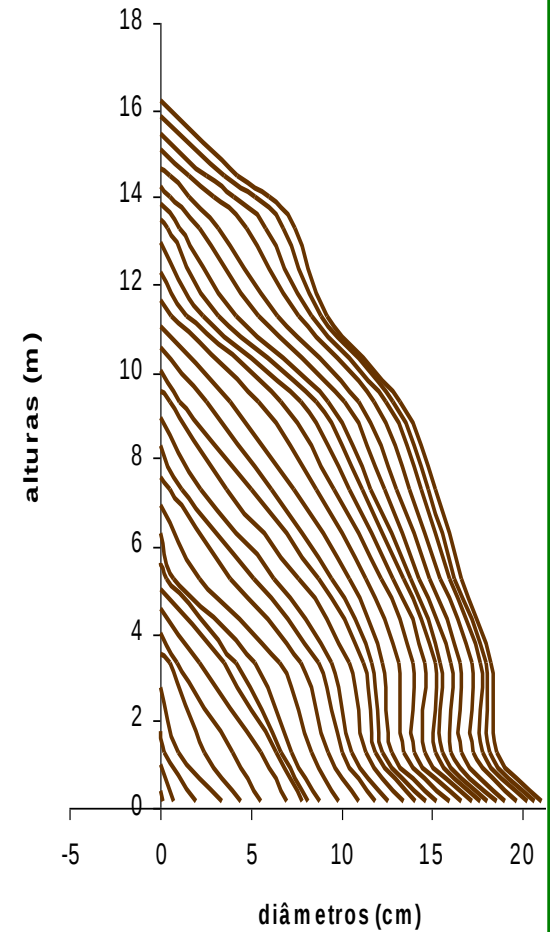
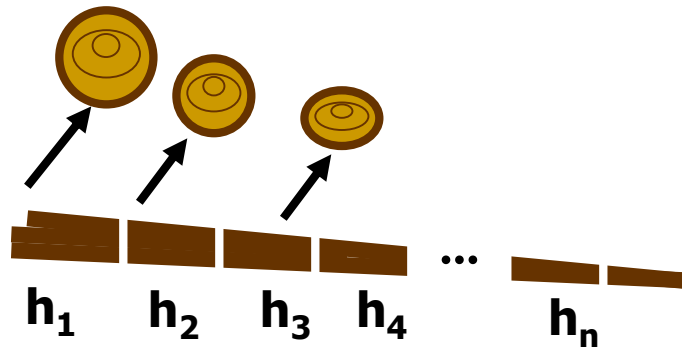
Diameter distributions



Stand volume



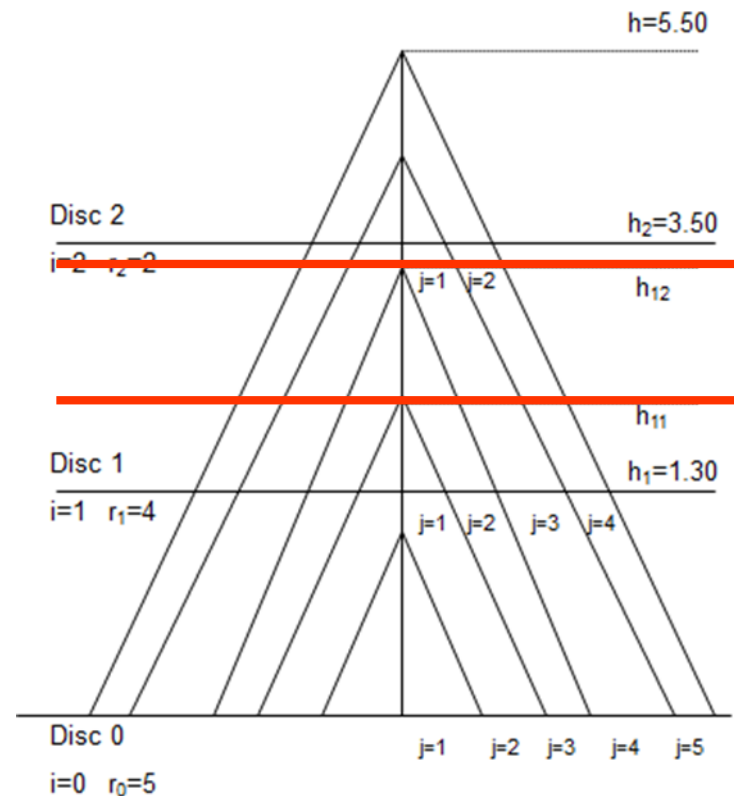
Stem analysis



Stem analysis - example

height	N rings	age
0	5	0
1.30	4	1+ ...
3.50	2	3+ ...
5.50	0	5

- ✗ Tree is 5 years old
- ✗ Between Disc 1 and Disc 2, the correction is needed to estimate the heights at the end of the years: h_{11} and h_{12}
- ✗ The method most used for this correction is the Carmean method



Stem analysis

Carmean's correction

- ✗ Carmen's method is based in two assumptions:
 1. Constant annual increment in height between two discs
 2. Each disc occurs at the mid-point between two whorls

Stem analysis

Carmean's correction

- ✗ The application of the method to the whorls between two discs implies:
 - ✓ Compute the annual increment $i_h = (h_2 - h_1) / (nrg_1 - nrg_2)$, where h_i and nrg_i are the height and the number of rings of disc_i
- ✗ Compute the height of the first whorl as:
 - ✓ $h_{i1} = h_i + i_h / 2$
- ✗ The heights of the following whorls are computed as:
 - ✓ $h_{ij} = h_i + i_h / 2 + (j - 1) * i_h = h_{i(j-1)} + i_h$

Stem analysis

Carmean's correction

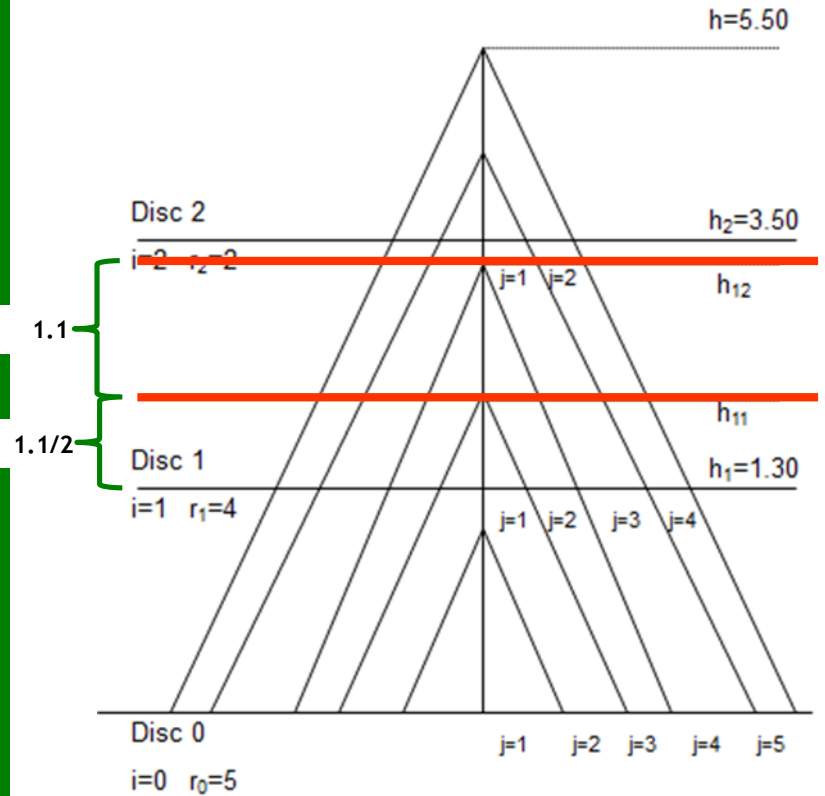
Let's compute h_{11} and h_{12} :

✖ Annual height growth:

$$i_h = (h_2 - h_1) / (4 - 2) = (3.50 - 1.30) / 2 = 1.1$$

✗ $h_{11}=1.30+1.1/2=1.85$

✗ $h_{12} = h_{11} + i_h = 1.85 + 1.1 = 2.95$



Stem analysis

Carmean's correction

✗ It is possible to obtain a general formula for the height of any whorl h_{ij} :

$$h_{ij} = h_i + \frac{1}{2} \frac{h_{i+1} - h_i}{r_i - r_{i+1}} + (j-1) \frac{h_{i+1} - h_i}{r_i - r_{i+1}}$$

$\frac{h_{i+1} - h_i}{r_i - r_{i+1}}$ is the annual growth between discs i and $i+1$

$$h_{11} = 1.30 + \frac{1}{2} \frac{3.50 - 1.30}{4 - 2} + (1-1) \frac{3.50 - 1.30}{4 - 2} = 1.30 + \frac{1}{2} 1.10 = 1.30 + 0.55 = 1.85$$

$$h_{12} = 1.30 + 0.55 + (2-1) 1.10 = 2.95$$

Stem analysis

Carmean's correction

